Viscosity of Gaseous HFC-143a (1,1,1-Trifluoroethane) Under High Pressures

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The viscosity of gaseous HFC-143a(1,1,1-trifluoroethane) was measured with an oscillating-disk viscometer of the Maxwell type at temperatures from 298.15 to 423.15 K and at pressures up to the saturated vapor pressure at each temperature under subcritical conditions or up to 9 MPa under supercritical conditions. Intermolecular potential parameters of HFC-143a for the extended corresponding states were determined from the viscosity data at 0.1 MPa. An empirical viscosity equation as functions of temperature and density is proposed to interpolate the present experimental results.

KEY WORDS: corresponding states; HFC-143a; viscosity.

1. INTRODUCTION

There has been a great interest in the thermophysical properties of HFC-143a (1,1,1-trifluoroethane), since it is considered to be an environmentally acceptable alternative for CFC-22 and CFC-502. Binary mixtures or ternary mixtures have also been recommended by the industry as potential alternatives. HFC-143a is one of the constituents in the mixture alternatives HFC-507 (49.91 % HFC-143a +50.09% HFC-125) and HFC-404A (52% HFC-143a + 44% HFC-125+4% HFC-134a).

Transport properties, such as viscosity and thermal conductivity, are essential in the analysis of mass and heat transfer processes in heat exchangers. Transport properties of the alternative refrigerants have a

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major impact on equipment design and thus influence the economical feasibility of heat exchangers which can actually approach the theoretical efficiency of the thermodynamic cycle with the ozone-depleting refrigerants.

In this paper, we present experimental results for the viscosity of gaseous HFC-143a under high pressures. The measurements were made at temperatures from 298.15 to 423.15 K and at pressures up to the saturated vapor pressure at each temperature under subcritical conditions or up to 9 MPa under supercritical conditions. The viscosity data at 0.1 MPa were applied to determine the scaling parameters of HFC-143a needed in the extended law of corresponding states. The data at high pressures were used to develop an empirical viscosity equation as functions of temperature and density.

The viscosity of HFC-143a in the liquid phase has been measured by few researchers $\lceil 1-6 \rceil$. The viscosity of HFC-143a in the gaseous phase at 298.15 K and at 0.1 MPa has been measured by Dunlop $[7]$. The gaseous viscosity of HFC-143a under high pressures, however, has not yet been measured.

2. EXPERIMENTS

The viscosity was measured with an oscillating-disk viscometer of the Maxwell type. The gas density at the experimental condition of the viscosity measurement was measured with a high-pressure gas pipette. The experimental apparatus and procedure were the same as those described in previous studies $[8-11]$. The apparatus constant at the experimental temperature and pressure conditions was determined by considering the viscosity data of nitrogen taken from Stephan et al. [12] and the nitrogengas density data from Jacobsen et al. [13]. Temperature and pressure values have an uncertainty of 0.01 K and 0.5 kPa. Density values have an uncertainty of $0.03 \text{ kg} \cdot \text{m}^{-3}$. The estimated error in the measurements of viscosity is within 0.3%.

The sample was supplied by Asahi Glass Co. Ltd. The purity of the sample, certified by the suppliers, was approximately 99.9 mol %. The sample was purified by distillation several times.

3. RESULTS

The experimental results for viscosity and density are presented in Table I and shown in Figs. 1 and 2. From Fig. 2, it can be seen that a negative initial density slope was observed for the viscosity isotherm at 298.15 K.

| P (MPa) | ρ (kg·m ⁻³) | η (μ Pa·s) |
|-----------|------------------------------|----------------------|
| | $T = 298.15$ K | |
| 0.1008 | 3.417 | 11.210 |
| 0.2138 | 7.248 | 11.199 |
| 0.3313 | 11.232 | 11.139 |
| 0.4482 | 16.433 | 11.119 |
| 0.5686 | 21.389 | 11.114 |
| 0.6866 | 26.446 | 11.110 |
| 0.8149 | 32.355 | 11.119 |
| 0.9223 | 37.623 | 11.146 |
| 1.0259 | 43.095 | 11.123 |
| 1.1361 | 49.822 | 11.153 |
| | $T = 323.15 K$ | |
| 0.1012 | 3.206 | 12.244 |
| 0.2914 | 9.453 | 12.236 |
| 0.4853 | 16.208 | 12.248 |
| 0.6808 | 23.257 | 12.248 |
| 0.8798 | 31.094 | 12.324 |
| 1.0730 | 39.248 | 12.359 |
| 1.2675 | 48.151 | 12.483 |
| 1.4714 | 58.307 | 12.566 |
| 1.6622 | 68.964 | 12.634 |
| 1.8536 | 80.976 | 12.785 |
| 2.1295 | 101.99 | 13.171 |
| 2.2388 | 111.86 | 13.428 |
| | $T = 348.15$ K | |
| 0.1021 | 2.992 | 13.209 |
| 0.3480 | 10.438 | 13.202 |
| 0.5918 | 18.194 | 13.235 |
| 0.8370 | 26.433 | 13.295 |
| 1.0797 | 35.106 | 13.345 |
| 1.3288 | 44.616 | 13.455 |
| 1.5663 | 54.371 | 13.547 |
| 1.7947 | 64.478 | 13.673 |
| 2.1489 | 81.812 | 13.968 |
| 2.4058 | 96.077 | 14.231 |
| 2.6358 | 110.54 | 14.559 |
| 3.0052 | 138.62 | 14.998 |
| 3.1921 | 156.55 | 15.799 |
| 3.4006 | 180.76 | 16.518 |
| 3.5503 | 203.23 | 17.332 |
| 3.6761 | 227.32 | 18.310 |

Table I. Viscosity of HFC-143a

| P (MPa) | ρ (kg·m ⁻³) | η (μ Pa·s) |
|-----------|------------------------------|----------------------|
| | $T = 373.15$ K | |
| 0.1024 | 2.792 | 14.109 |
| 0.3540 | 9.848 | 14.131 |
| 0.6500 | 18.494 | 14.249 |
| 0.9424 | 27.484 | 14.284 |
| 1.2369 | 37.031 | 14.332 |
| 1.5304 | 47.073 | 14.457 |
| 1.8252 | 57,874 | 14.618 |
| 2.1531 | 70.733 | 14,794 |
| 2.4257 | 82.174 | 14.920 |
| 2.7295 | 96.042 | 15.172 |
| 3.0476 | 111.84 | 15.532 |
| 3.4078 | 131.95 | 16.045 |
| 3.7359 | 152.60 | 16.630 |
| 4.0178 | 172.61 | 17.265 |
| 4,2694 | 192.44 | 17.956 |
| 4.4937 | 212.81 | 18.704 |
| 4.6911 | 232.75 | 19.488 |
| 4.8091 | 246.55 | 20.047 |
| 4.9729 | 266.33 | 20.902 |
| 5.1226 | 284.81 | 21.852 |
| | $T = 398.15$ K | |
| 0.1008 | 2.573 | 15.045 |
| 0.4013 | 10.433 | 15.094 |
| 0.7081 | 18.761 | 15.137 |
| 1.0483 | 28.394 | 15.249 |
| 1.4405 | 40.057 | 15.342 |
| 1.8319 | 52.419 | 15.516 |
| 2.2396 | 66.180 | 15.752 |
| 2.6129 | 79.464 | 15.975 |
| 3.0119 | 94.748 | 16.300 |
| 3.4817 | 114.30 | 16.765 |
| 3.9126 | 133.76 | 17.311 |
| 4.3645 | 156.32 | 17.987 |
| 4.7136 | 175.64 | 18.600 |
| 5.0323 | 194.06 | 19.224 |
| 5.3288 | 212.67 | 19.936 |
| 5.6721 | 235.79 | 20.879 |
| 5.9702 | 257.26 | 21.797 |
| 6.3416 | 285.09 | 23.106 |
| 6.6684 | 311.10 | 24.450 |
| 6.8054 | 326.46 | 25.246 |
| | | |

Table I. (Continued)

| $n(\mu Pa \cdot s)$ | ρ (kg·m ⁻³) | P (MPa) |
|---------------------|------------------------------|-----------|
| | $T = 423.15$ K | |
| 16.050 | 2.484 | 0.1035 |
| 16.150 | 12.114 | 0.4959 |
| 16.222 | 22.081 | 0.8847 |
| 16.355 | 33.747 | 1.3219 |
| 16.547 | 47.916 | 1.8270 |
| 16.788 | 63.228 | 2.3431 |
| 17.098 | 77.748 | 2.8014 |
| 17.508 | 96.391 | 3.3575 |
| 17.937 | 114.35 | 3.8601 |
| 18.541 | 135.99 | 4.4243 |
| 19.093 | 152.56 | 4.8321 |
| 19.709 | 172.25 | 5.2869 |
| 20.655 | 197.32 | 5.8436 |
| 21.542 | 220.27 | 6.3019 |
| 22.664 | 246.94 | 6.8185 |
| 24.031 | 276.36 | 7.3580 |
| 25.431 | 302.04 | 7.8603 |
| 27.245 | 336.64 | 8.4453 |
| 28.550 | 362.21 | 8.8523 |
| | | |

Table I. (Continued)

Fig. 1. Viscosity of HFC-143a as a function of pressure.

Fig. 2. Viscosity of HFC-143a as a function of density.

The low-pressure gas viscosity can be represented by the Chapman-Enskog equation derived from the kinetic theory for dilute gases:

$$
\eta_0 = \frac{5}{16} \frac{(MkT)^{0.5}}{(\pi N)^{0.5}} \frac{f_\eta}{\sigma^2 \Omega^{(2,2)^*}(T^*)}
$$
(1)

In Eq. (1), k is Boltzmann's constant, M is the molar mass in kg \cdot kmol $^{-1}$, *N* is Avogadro's number, $\Omega^{(2,2)*}$ *(T^{*})* is the collision integral, f_n is the higher-order correction factor for viscosity, $T^* = kT/c$ is the reduced temperature, T is the absolute temperature, η_0 is the gas viscosity at 0.1 MPa in μ Pa·s, and ε and σ are the characteristic scaling parameters. Based on accurate experimental data for the second virial coefficient and gaseous viscosity of noble gases, Kestin et al. [14-16] developed an extended corresponding states principle, which is a most powerful method to predict transport properties of pure gases and gaseous mixtures at normal pressure. As for the collision integral and correction factor, we have used the following equation presented by Kestin et al. $[16]$:

$$
\Omega^{(2, 2)*}(T^*) = \exp[0.46641 - 0.56991 \ln T^* + 0.19591(\ln T^*)^2 -0.03879(\ln T^*)^3 + 0.00259(\ln T^*)^4]
$$
 (2)

Table II. Potential Parameters for HFC-143a and Deviation of Experimental Viscosity at 0.1 MPa from Eq. $(1)^{a}$

| 365.58 K |
|-----------|
| 0.4885 nm |
| 0.19% |
| 0.45% |
| |

^a Average deviation = 100 $|\eta_{0.exp} - \eta_{0.ext}|/n_{0.ext}$ Maximum deviation = max of 100 $|\eta_{0.~exp} - \eta_{0.~cal}|/\eta_{0.~cal}$. $n =$ number of data.

and

$$
f_{\eta} = 1 + 3(8E^* - 7)^2/196\tag{3}
$$

where E^* can be obtained from the following equation:

$$
E^* = 1 + \frac{T^*}{4} \frac{d \ln \Omega^{(2,2)*}}{dT^*}
$$
 (4)

The values of the scaling parameters, σ and ε , can be determined from the gas viscosity data at 0.1 MPa. For the gas viscosity at 298.15 K and 0.1 MPa, the present result is about 1 % lower than the viscosity value of Dunlop [7]. Therefore, we used the present results only for the determination of the scaling parameters. The optimum values of the parameters σ and ε and the deviations of the calculated values from Eq. (1) are given in Table II. The present viscosity data can be represented well by Eq. (1) with the values of the scaling parameters in Table II, with a maximum deviation of 0.45% and an average deviation of 0.19% (Fig. 3).

Fig. 3. Deviations of experimental viscosity values of HFC-143a at 0.1 MPa from those calculated with Eq. (1) .

Fig. 4. Deviations of experimental viscosity values of HFC-I43a at high pressures from those calculated with Eq. (5).

For the gas viscosity η at temperature T and at high pressures, we developed the following empirical viscosity equation as a function of temperature and density:

$$
\eta = \eta_0 + a_0(\rho - \rho_0) + a_1(\rho - \rho_0)^2 \tag{5}
$$

with

$$
a_0 = -0.0254485 + 8.03031 \times 10^{-5} T \tag{6}
$$

$$
a_1 = 1.29211 \times 10^{-4} - 1.28578 \times 10^{-7} T \tag{7}
$$

where η_0 is the gas viscosity at 0.1 MPa represented by Eq. (1), ρ is the gas density at high pressures in kg m^{-3} , ρ_0 is the gas density at 0.1 MPa in kg \cdot m⁻³, and *T* is the absolute temperature in K. The values of the coefficients in Eqs. (6) and (7) were determined from a least-squares fit of Eq. (5) to the present experimental viscosity values. Figure 4 shows the deviations of the present results from Eq. (5). As can be seen from Fig. 4, Eq. (5) represents the present results with an average deviation of 0.49% and a maximum deviation of 1.6%. It should be noted that Eq. (5) should not be used outside the temperature and density ranges of this study.

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